

2nd Workshop on Long-term Human Motion Prediction

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Exploration/Exploitation in Path Planning Using Probability Propagation *

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$$f(s_1, a_1) = \pi(s_1, a_1);$$

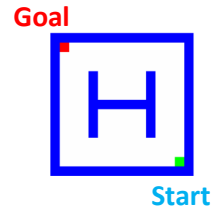
$$f(s_t, a_t) =$$

$$\sum_{a_{t-1}} p(a_t | s_t, a_{t-1}) \sum_{s_{t-1}} p(s_t | s_{t-1}, a_{t-1}) f(s_{t-1}, a_{t-1})$$

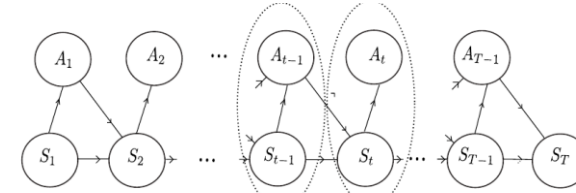
$$f(s_T) = \sum_{a_{T-1}} \sum_{s_{T-1}} p(s_T | s_{T-1}, a_{T-1}) f(s_{T-1}, a_{T-1});$$

$$b(s_{T-1}, a_{T-1}) \propto \sum_{s_T} p(s_T | s_{T-1}, a_{T-1}) b(s_T);$$

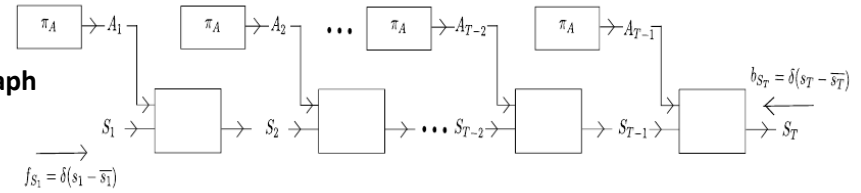
$$b(s_{t-1}, a_{t-1}) \propto \sum_{a_t} p(a_t | s_t, a_{t-1}) \sum_{s_t} p(s_t | s_{t-1}, a_{t-1}) b(s_t, a_t) \quad t = T - 1 : 2$$



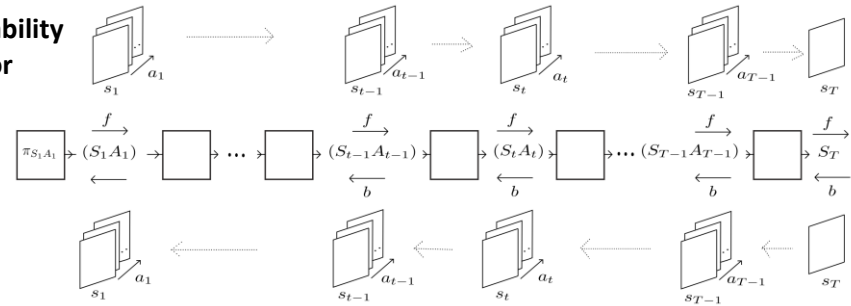
Bayesian Graph



Factor Graph



Probability Tensor Flow



Pure Diffusion

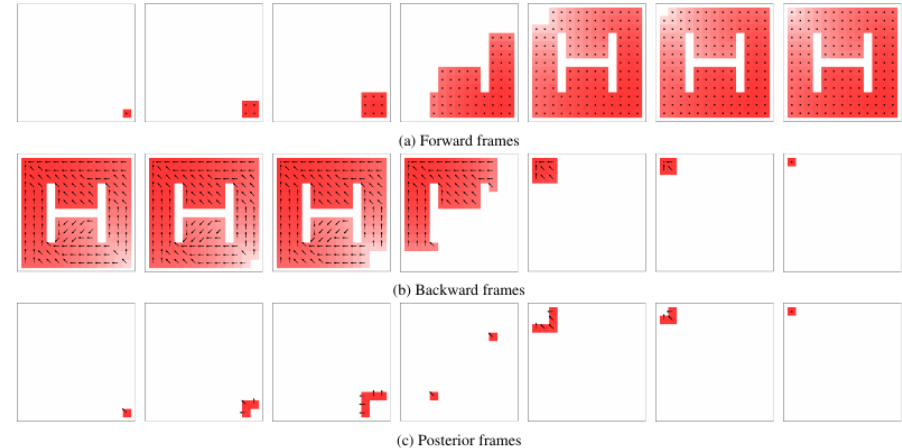
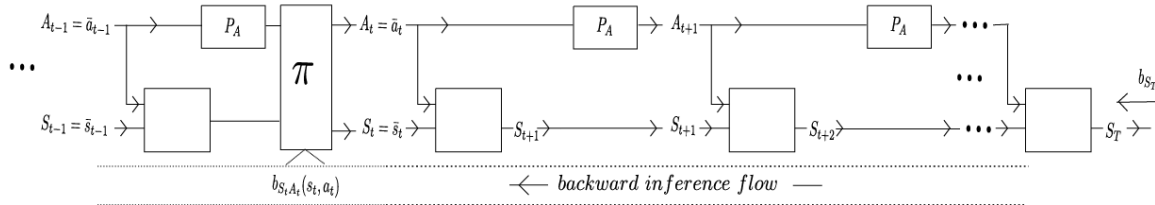


Fig. 2: Flows. From left to right, the snaps are taken at time $t = 1, t = 2, t = 3, t = 10, t = 18, t = 19, t = T = 20$

Introducing control using the backward flow



Known MAP and Goal

G-algorithm Outline:

- Initialize state (goal) at time $t = T$ with $b_{S_T}(s_t) = \delta(s - \bar{g})$;
- Compute the complete backward flow using the last two equations in (4) from $t = T$ to $t = 2$;
- Initialize the state and action (start) at time $t = 1$ with $f_{S_1 A_1}(s_1, a_1) = \delta(s_1 - \bar{s}, a_1 - \bar{a})$;
- Set $t \leftarrow t + 1$ and compute the forward distribution $f_{S_t A_t}(s_t, a_t)$ using the second equation in (4);
- Compute the posterior distribution:

$$p_{S_t A_t}(s_t, a_t) \propto f_{S_t A_t}(s_t, a_t) b_{S_t A_t}(s_t, a_t);$$
- Set $(S_t, A_t) = (\bar{s}_t, \bar{a}_t) = \operatorname{argmax} p_{S_t A_t}(s_t, a_t)$
- Replace forward distribution as:

$$f_{S_t A_t}(s_t, a_t) = \delta(s_t = \bar{s}_t, a_t = \bar{a}_t)$$
- Back to (d) for the next time step.



The algorithm essentially maximizes the likelihood in a greedy fashion. The solution is reached much like in the Viterbi algorithm (poor man's Viterbi) in a large-dimensional space. Therefore, if the time horizon is set to minimum time, the solution is optimal.

Extended to multiple agents:

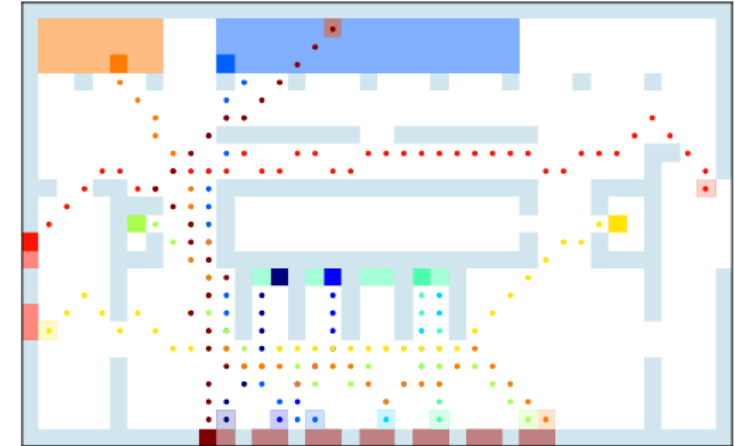


Figure 1. Agents move in a train station-like environment from their starting positions to their goals

- [13] Francesco A.N. Palmieri, Krishna R. Pattipati, Giovanni Fioretti, Giovanni Di Gennaro, and Amedeo Buonanno, "Path Planning Using Probability Tensor Flow," *arXiv:2003.02774*, sub. for journal publication, II review, 2020.

No knowledge of the map and limited visibility

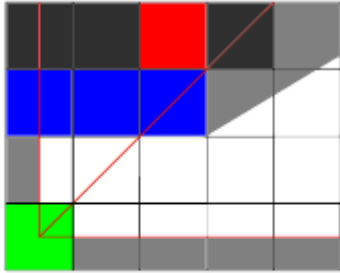


Figure 2. Agent's viewing geometry. The agent (green) looks at 315° (counterclockwise angles) with 90° viewing aperture. Because of the presence of the obstacles (blue), the goal (red) is not visible. The black areas are the invisible regions. We assume that a partially visible cell is visible (gray).

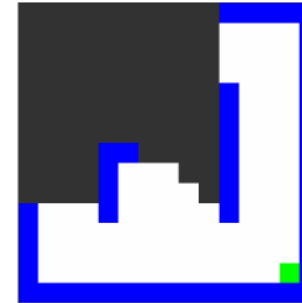
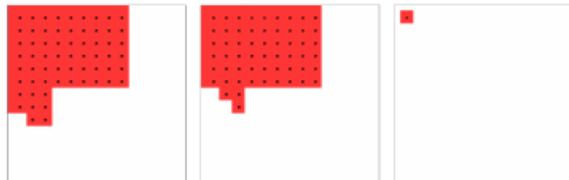


Fig. 10: Limited visibility. The black zone represents the area of the map the agent doesn't know yet.

The unknown map becomes a distributed goal



(a) Exploration frames



(b) Goals exploration frames

Fig. 11: Exploration. The frames show the position of the agent and the known area at $t = 10$, $t = 11$ and $t = 12$.

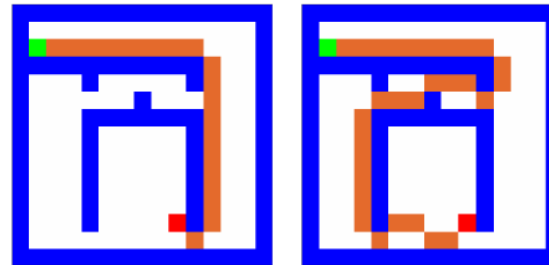
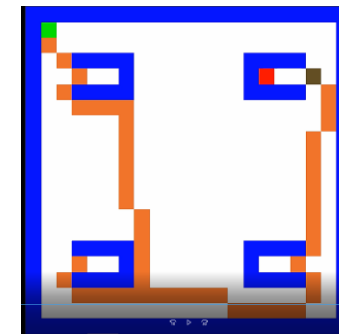
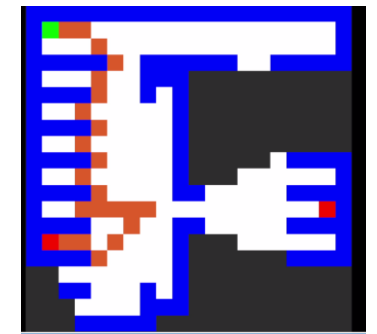


Figure 4. Paths obtained with a fully known map (left) and after exploration due to limited view (right)

Animations



Hidden target



Parking lot

Films available at the poster session, or on our website

<https://www.mlsplab-unicampania.it/research/topics/path-modeling.html>